Estimation of LLE Data for Binary Systems of \textit{N-Formylmorpholine} with Alkanes Using Artificial Neural Network–Genetic Algorithm (ANN–GA) Model

Reza Beigzadeh
Department of Chemical Engineering, Faculty of Engineering, University of Kurdistan, Sanandaj, Iran

\textbf{ARTICLE INFORMATION}

Received: 24 May 2018  
Received in revised: 22 August 2018  
Accepted: 10 September 2018  
Available online: 10 September 2018

\textbf{KEYWORDS}

Artificial neural network (ANN)  
Binary system  
Genetic algorithm (GA)  
Liquid-liquid Equilibrium (LLE)  
\textit{N-Formylmorpholine}

\textbf{ABSTRACT}

The purpose of this work was to predict liquid-liquid equilibrium of binary systems including \textit{N-formylmorpholine} (NFM) with alkanes (heptane, nonane, and 2,2,4-trimethylpentane) over the temperature range from around 300 K to 420 K. Therefore, three feed-forward artificial neural network (ANN) models were developed for the three systems. Compositions of alkanes in light phase and heavy phase were considered as network inputs, and the temperature was the output variable. Genetic algorithm (GA) method was used to design the neural network. It minimized the total mean squared error (MSE) between net output and desired output with optimizing weights and biases of the ANN. The validity of the models was evaluated through a test data set, which was not used in the training data set. The results of this work show that the hybrid of artificial neural network and genetic algorithm (ANN–GA) can estimate the LLE of the binary systems with high precision.
Graphical Abstract

Introduction

Separation processes are one of the most important operations in chemical processes. In the petroleum industry, separation of aromatic hydrocarbons from aliphatic hydrocarbons has great importance. The common process for these separations is liquid-liquid extraction [1]. For extraction of aromatics, many solvents such as sulfolane [2–5], glycol [6, 7], N-formylmorpholine (NFM) [8–10] and combinations of the solvents [11] have been used. In the petroleum industry, there is much attention to morpholine derivatives e.g. N-methylmorpholine, hydroxyethyl morpholine, N-acetylmorpholine, N-formylmorpholine (NFM) and phenylmorpholine because of their high effectiveness on the recovery of aromatics [12]. N-formylmorpholine (NFM) as an extraction solvent is widely used to separate aromatic hydrocarbons from aliphatic. NFM has low viscosity, good fluidity and good thermal stability [1]; also, it minimizes aromatic content in
gasoline and refines the extracted aromatics. Thus, NFM plays an important role in liquid extraction and has a model for predicting phase equilibrium and thermodynamic properties of systems containing morpholine whose derivatives are essential.

For a better understanding of their thermodynamic behavior and for the development of the model, trustworthy experimental phase equilibrium data are needed. Therefore, several researchers started with measurements of the required properties of the liquid-liquid equilibrium. Some LLE data of binary systems including NFM with n-alkanes [8-13] and cycloalkanes [10] and some of the ternary systems including NFM, aromatics, and alkanes [14-17] have been investigated. Some experimental LLE data for a mixed solvent system (N-formylmorpholine + sulfolane, n-hexane and benzene) over the temperature range of 298.15 to 318.15 K were determined by J. Mahmoudi and M.N. Lotfollahi [18]. The LLE data of NFM with aromatics, n-hexane, n-heptane and water at different temperatures from 293 to 333 K were obtained by Cincotti et al. [8]. The LLE results for the ternary mixture of (NFM + 2,2,4-trimethylpentane + ethylbenzene) at temperatures 303.15, 313.15, and 323.15 K were investigated by Z. Wang et al. [1]. However, according to the importance of NFM, the liquid-liquid equilibrium data are still comparatively scarce for the binary systems containing NFM in the studies; and a mathematical model with the aim of contributing to the knowledge of liquid-liquid equilibrium with NFM can be so useful. There are limited empirical correlations for predicting LLE characterization. On the other hand, the artificial neural network (ANN) models on VLE data in several subjects have been carried out [19-21] but there are limited studies on LLE data using ANN models.

The aim of this work is to predict LLE properties for the binary systems including N-formylmorpholine with alkanes using the feed-forward ANN model, trained by back propagation algorithm (BP), and genetic algorithm (GA). The GA technique was used for optimizing the initial weights and biases of the back-propagation network. It minimizes the total mean squared error (MSE) between the output of the developed ANN and desired output with optimizing weights and biases of the ANN [22]. In this respect, three artificial neural network models have been carried out on the LLE data of binary systems {heptane (1) + NFM (2)}, {nonane (1) + NFM (2)} and {2,2,4-trimethylpentane (1) + NFM (2)}. Compositions of component 1 in light phase and heavy phase were considered as network inputs, and the temperature was the output variable as the target of the model. Z. Wang et al. [23] applied the experimental values of the LLE data. By using a large number of parameters (weights and biases), the ANN is a suitable method for estimating flexible mathematical functions. In this work, the hybrid artificial neural network and genetic algorithm were used to obtain global convergence with a high accuracy and avoid a local answer.
Experimental

Hybrid neural networks and genetic algorithm

Artificial neural networks (ANNs) which are collections of flexible mathematical functions imitate biological systems using a number of interconnected artificial neurons to recognize complex and nonlinear relationships [24]. Because of this ability of the ANNs, they can be used in various fields of chemical engineering [25]. The ANN learns the data pattern using the “training” algorithms. These methods are extremely useful in recognizing templates in complex data by providing nonlinear equations between inputs and outputs of the network. Each neuron of the network is connected with a weight to the other neurons via direct communication bonds, which finally provides a reasonable relationship between input and output values. The output of each neuron generated by summation of weighed inputs plus bias under a transfer function. In common, ANNs are parallel organized structures that comprised of interconnected neurons as input layer (independent variables), one or more hidden layers, be located between them, and an output layer (dependent variables) [26] as shown in Figure 1. The number of neurons of the input and output layers is usually determined by the number of input and output variables (U and Y), respectively. However, the number of neurons in the hidden layers is changeable and it is important for optimization of the network, which will be studied in the following sections.

For developing the model to predict characteristics of LLE, The following steps are required: The first step in designing artificial neural network models, which is one of the most important decisions in the development of the neuromorphic model, is to prepare an adequate database to train the network and to evaluate its capacity for generalization [27]. The next step is data preprocessing. It is a normalization procedure for presenting the input data to the network and set the data between the largest data as 1 and the smallest one as zero number. The third step is network structure. In this part, the number and type of network layers, number of neurons in layers, and the selection of transfer functions are determined. The next step in designing ANN is training. Training of the network means adjusting the weights and biases in order to make the network outputs closer to the aim values. The most commonly used neural network training algorithm is a back propagation algorithm (BP algorithm). This algorithm has the main defect in training because of its random choice in weights and biases. It may cause trapping into local minimum and converge slowly [27]. There are many global search skills to overcome these disadvantages. One of the most effective techniques that used for optimizing the initial weights and
Biases of the BP network is the genetic algorithm (GA) [28]. In this work, the initial weights and biases of the artificial neural network were optimized using this method.

GA is an extremely important method in optimization inspired by Darwinian biological evolution principle, which is quite popular in engineering optimization. The optimization procedure involves selection, elitism, crossover, and mutation operations and starts with a set of random solution (population) and develops through continuous iterations (generations) for getting better solutions [27-29]. In brief, GA uses four steps to obtain the optimum weights of ANN as follows [22-30]:

- Generate random initial population of chromosomes (weights and biases).
- Evaluate the fitness values (objective function value) of solutions (computing their performance error).
- Represent new generation by selection, elitism, crossover, and mutation.
- Use new population for the next generation. The same procedure is repeated for next generations and the algorithm is run for a limited number of cycles. The final set of weights and biases was designated as the result of GA and they are saved for BP training. After the GA training, the BP algorithm starts using the solution supplied by GA [22].

**Figure 1.** Topology of three-layer back propagation artificial neural network used in this study.
Figure 2. Flowchart of the artificial neural network–genetic algorithm (ANN-GA) model
The final step in designing ANN is to test the performance of the model. At this step, test data are used in the ANN model and in order to evaluate the performance of the model, the mean relative error (MRE) and the mean square error (MSE) between the experimental and estimated values were measured. Figure 2. shows the flow chart of the artificial neural network–genetic algorithm (ANN–GA) model which has been used in this work.

**Developing correlations using ANN-GA modeling and training**

The ANN that is used in this study is a multilayer feed-forward neural network with the Levenberg-Marquardt algorithm [31-33] for the correction of the weights and a learning order of the back propagation (BP) of errors.

The experimental LLE data for three mixtures composed of N-formylmorpholine (NFM) with alkanes (heptane, nonane, and 2,2,4-trimethylpentane) over the temperature range from around 300 K to 420 K, were measured by Wang et al. [23] and were used for training and testing the ANN-GA model. The investigated systems were at the equilibrium condition. There were two components in each of the systems, N-formylmorpholine (NFM) with an alkane. In this study, the ANN was developed for predicting temperature (output data) as a function of mole fraction of alkane in light phase ($X_{11}$) and mole fraction of alkane in heavy phase ($X_{12}$) (input data). Before the training of the ANNs, because of the different range sizes between input and output data, it is usually common to normalize input and output data. So, all data were normalized in the range of 0-1 in order to avoid any computational difficulty, using the following relation:

$$\text{Normalized data} = \frac{\text{data value} - \text{minimum value}}{\text{maximum value} - \text{minimum value}}$$

The next step after determining the input and output is to develop the ANN architecture. An ANN with one hidden layer was chosen as the network structure. Theoretical procedures for obtaining the appropriate number of hidden layer are not available. Therefore, the trial and error method was used to determine the number of neurons in the layer. Increasing the number of neurons in hidden layer may bring over fitting. So normally a small number of neurons were chosen for the hidden layer and if the deviation of the trained ANN model does not reach to the optimal tolerance, the number of neurons in the hidden layer was increased and estimation of performance is repeated [34]. Therefore, two numbers of neurons were decided for the hidden layer. This number was obtained through experience, so that the deviation of the trained model is in optimal tolerance.
In the neural network model, the final output of the ANN is obtained from the following relationship [35]:

\[
Y = F_l \left( \sum_{j=1}^{m} W_{kj} \left[ F_i \left( \sum_{i=1}^{n} W_{ji} U_i + b_j \right) \right] + b_k \right)
\]

(2)

where \( Y, U, m, n \) are the final answer of the network, the input value of the network, the number of input variables and the number of neurons; \( i, j, k \) refer to the input, hidden, and output layer, respectively. In this study, the “hyperbolic tangent sigmoid” transfer function was chosen for the hidden layer and “linear” function was considered for the output layer. These functions are defined as follows:

\[
F_i(x) = \frac{2}{1 + e^{-2x}} - 1
\]

(3)

\[
F_l(x) = x
\]

(4)

As mentioned for training networks, random initial weights and biases may cause trapping into local minima and converge slowly. So in this study, GA searching approach was used for solving problems on which traditional methods do not succeed to achieve the global optimum result (minimum or maximum). Based on results, the best population size in the case studied here was found to be 100. The crossover probability and mutation probability are determined and their values were found to be 0.8 and 0.01, respectively. The GA would stop after the end of 300 generations because it had almost reached optimal values.

For evaluating the validity of the model, the data points were divided randomly into two parts, the first data set (around 70% of input data) was selected for training the network and the second data set (remaining data) was employed for testing the model.

**Results and discussion**

In the present study, three ANN–GA models were developed for three LLE systems. The experimental liquid-liquid equilibrium data for the three binary systems (nonane + NFM), (2,2,4-trimethylpentane + NFM) and (heptane + NFM), are represented in Tables 1 to 3, respectively. The ANN–GA is trained with randomly 70 percent of data points and the rest data points considered as the test data points. Before being fed into ANN-GA model, because of difference in magnitude and dimension of experimental data, it was normalized.
Table 1. Experimental LLE data of temperature at the mole fraction of light phase $x_{11}$ and heavy phase $x_{12}$ for the system \{Nonane (1) + NFM (2)\} \[11\]

<table>
<thead>
<tr>
<th>T/K</th>
<th>Light phase $x_{11}$</th>
<th>Heavy phase $x_{12}$</th>
<th>T/K</th>
<th>Light phase $x_{11}$</th>
<th>Heavy phase $x_{12}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>303.15</td>
<td>0.9801</td>
<td>0.0118</td>
<td>365.85</td>
<td>0.8952</td>
<td>0.0226</td>
</tr>
<tr>
<td>312.95</td>
<td>0.9661</td>
<td>0.0148</td>
<td>370.95</td>
<td>0.8841</td>
<td>0.0289</td>
</tr>
<tr>
<td>320.65</td>
<td>0.9572</td>
<td>0.0176</td>
<td>392.45</td>
<td>0.8344</td>
<td>0.0346</td>
</tr>
<tr>
<td>327.97</td>
<td>0.9484</td>
<td>0.0192</td>
<td>402.15</td>
<td>0.8107</td>
<td>0.0347</td>
</tr>
<tr>
<td>334.95</td>
<td>0.942</td>
<td>0.0212</td>
<td>409.65</td>
<td>0.8344</td>
<td>0.0386</td>
</tr>
<tr>
<td>343.04</td>
<td>0.9322</td>
<td>0.0219</td>
<td>370.95</td>
<td>0.8841</td>
<td>0.0373</td>
</tr>
<tr>
<td>349.4</td>
<td>0.9134</td>
<td>0.0311</td>
<td>399.65</td>
<td>0.7595</td>
<td>0.047</td>
</tr>
<tr>
<td>350.65</td>
<td>0.9236</td>
<td>0.0202</td>
<td>427.85</td>
<td>0.7621</td>
<td>0.0433</td>
</tr>
<tr>
<td>356.95</td>
<td>0.9098</td>
<td>0.0213</td>
<td>370.95</td>
<td>0.8841</td>
<td>0.047</td>
</tr>
</tbody>
</table>

Table 2. Experimental LLE data of temperature at the mole fraction of light phase $x_{11}$ and heavy phase $x_{12}$ for the system \{2,2,4-trimethylpentane (1) + NFM (2)\} \[11\]

<table>
<thead>
<tr>
<th>T/K</th>
<th>Light phase $x_{11}$</th>
<th>Heavy phase $x_{12}$</th>
<th>T/K</th>
<th>Light phase $x_{11}$</th>
<th>Heavy phase $x_{12}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>307.85</td>
<td>0.9705</td>
<td>0.0193</td>
<td>355.55</td>
<td>0.8838</td>
<td>0.0316</td>
</tr>
<tr>
<td>312.55</td>
<td>0.9673</td>
<td>0.022</td>
<td>365.25</td>
<td>0.8677</td>
<td>0.0382</td>
</tr>
<tr>
<td>318.85</td>
<td>0.964</td>
<td>0.0248</td>
<td>374.55</td>
<td>0.8426</td>
<td>0.0417</td>
</tr>
<tr>
<td>323.64</td>
<td>0.9577</td>
<td>0.0263</td>
<td>383.75</td>
<td>0.804</td>
<td>0.0413</td>
</tr>
<tr>
<td>329.33</td>
<td>0.9542</td>
<td>0.0273</td>
<td>391.65</td>
<td>0.7784</td>
<td>0.0428</td>
</tr>
<tr>
<td>334.85</td>
<td>0.9447</td>
<td>0.0289</td>
<td>399.65</td>
<td>0.7595</td>
<td>0.047</td>
</tr>
<tr>
<td>342.5</td>
<td>0.9313</td>
<td>0.0298</td>
<td>408.45</td>
<td>0.7401</td>
<td>0.0504</td>
</tr>
<tr>
<td>349.4</td>
<td>0.9134</td>
<td>0.0311</td>
<td>383.75</td>
<td>0.8426</td>
<td>0.0413</td>
</tr>
</tbody>
</table>

Table 3. Experimental LLE data of temperature at the mole fraction of light phase $x_{11}$ and heavy phase $x_{12}$ for the system \{heptane (1) + NFM (2)\} \[11\]

<table>
<thead>
<tr>
<th>T/K</th>
<th>Light phase $x_{11}$</th>
<th>Heavy phase $x_{12}$</th>
<th>T/K</th>
<th>Light phase $x_{11}$</th>
<th>Heavy phase $x_{12}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>298.75</td>
<td>0.9794</td>
<td>0.0183</td>
<td>348.35</td>
<td>0.9527</td>
<td>0.0399</td>
</tr>
<tr>
<td>302.85</td>
<td>0.9688</td>
<td>0.0216</td>
<td>357.75</td>
<td>0.9467</td>
<td>0.0446</td>
</tr>
<tr>
<td>312.05</td>
<td>0.9645</td>
<td>0.0243</td>
<td>369.35</td>
<td>0.9279</td>
<td>0.0536</td>
</tr>
<tr>
<td>320.05</td>
<td>0.9624</td>
<td>0.0277</td>
<td>378.3</td>
<td>0.9087</td>
<td>0.0667</td>
</tr>
<tr>
<td>329.35</td>
<td>0.9605</td>
<td>0.0323</td>
<td>389.35</td>
<td>0.8819</td>
<td>0.0804</td>
</tr>
<tr>
<td>337.65</td>
<td>0.9575</td>
<td>0.038</td>
<td>389.35</td>
<td>0.8819</td>
<td>0.0804</td>
</tr>
</tbody>
</table>

The ANNs had one hidden layer and the number of neurons in the hidden layer was evaluated by the use of a trial and error method. A large number of neurons in hidden layer can cause overfitting in which the model can perfectly predict the training data, but it is unable to sufficiently predict the test data set. The optimal number of neurons in the hidden layer should be determined. In this study, various numbers of neurons were tested for the hidden layer, and the optimal number of
neurons was evaluated. The deviation, which was used for choosing the best ANN architecture, is the mean square error (MSE) defined as follow:

\[ MSE = \frac{1}{N} \sum_{i=1}^{N} (t_i - y_i)^2 \]  

(5)

Where N is the number of data points, t is the target (experimental) data, and y is the estimated value.

The results of the method for achieving the optimum number of neurons in the hidden layer have been presented in Figure 3. In the Figure, MSE values of different ANN configurations, of each the three networks, for estimation of T are presented. The configuration with minimum error (MSE) is determined as the best network architecture. According to Figure 3, the best network configuration has one hidden layer with two neurons. The minimum MSE values of the ANN for the prediction of system temperature were 0.5168, 2.7606 and 0.5034, for (nonane + NFM), (heptane + NFM) and (2,2,4-trimethylpentane + NFM) systems, respectively.

![Figure 3. MSE values for different number of hidden neurons in the developed ANNs](image)

Hence, for the three LLE systems, the final output of the ANN-GA via input compositions can be obtained using the parameters (weights and biases) of the selected ANN architecture in Eq. (2), as follows:
nonane (1) + NFM (2):  
\[ T = -0.4015F_1 \left[ 1.9987 x_{11} - 0.2597 x_{12} - 0.0777 \right] \\
+ 0.3029 F_1 \left[ -4.4314 x_{11} + 0.2642 x_{12} + 3.7356 \right] \\
+ 0.5669 \]  \tag{6}

-{2,2,4-trimethylpentane (1) + NFM (2)}:  
\[ T = 0.2648 F_1 \left[ -3.8521 x_{11} + 1.8823 x_{12} + 3.1788 \right] \\
- 0.3842 F_1 \left[ 1.5114 x_{11} - 1.0019 x_{12} - 0.3842 \right] \\
+ 0.5234 \]  \tag{7}

{-heptane (1) + NFM (2)}:  
\[ T = -0.4280 F_1 \left[ 3.1796 x_{11} - 2.0468 x_{12} - 2.0153 \right] \\
- 0.3662 F_1 \left[ 1.7517 x_{11} - 0.2434 x_{12} + 0.6428 \right] \\
+ 0.7121 \]  \tag{8}

It should be noted that input and output data are in normalized range (Eq. 1). Table 4. reports the MSE and MRE values of the systems with optimum hidden neurons and same iterations. The MSE equation mentioned as Eq. (5) and mean relative errors (MRE) calculated as follows:

\[ MRE(\%) = \frac{100}{N} \sum_{i=1}^{N} \left( \frac{t_i - y_i}{t_i} \right) \]  \tag{9}

Where N, t and y parameters are the number of data points, the target (experimental) data, and the estimated value, respectively, alike in MSE equation.

**Table 4.** Best MSE and MRE values of different training algorithm for ANNs with 2-2-1 configuration

<table>
<thead>
<tr>
<th>Training algorithm</th>
<th>Nonane (1) + NFM (2)</th>
<th>2,2,4-trimethylpentane(1) + NFM (2)</th>
<th>heptane (1) + NFM (2)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>MSE</td>
<td>MRE (%)</td>
<td>MSE</td>
</tr>
<tr>
<td>Trainlm</td>
<td>0.5168</td>
<td>0.1365</td>
<td>0.5034</td>
</tr>
<tr>
<td>Traincgb</td>
<td>2.3993</td>
<td>0.3292</td>
<td>11.1145</td>
</tr>
<tr>
<td>Trainbr</td>
<td>4.4419</td>
<td>0.4992</td>
<td>5.8544</td>
</tr>
<tr>
<td>Traingda</td>
<td>68.52</td>
<td>2.3190</td>
<td>96.31</td>
</tr>
</tbody>
</table>

In additions, these errors reported for various training algorithms including Levenberg–Marquardt algorithm (trainlm), conjugate gradient back–propagation with Powell–Beale restarts (traincgb),
bayesian regularization back-propagation (trainbr), and gradient descent with adaptive learning rate back-propagation (traingda). The obtained errors in this table revealed that using the Levenberg-Marquardt algorithm (trainlm) leads to the best answer.

The comparison between the simulation results for prediction of temperature for the developed ANN-GA and the experimental training data points is illustrated in Figure 4. It is tried to illustrate the validity of the model in the prediction of the temperature for \{\text{nonane (1) + NFM (2)}\} mixture. The best fit, that output is equal to targets, is appeared by the solid line. Figure 4. shows a good correlation between the ANN predictions and the experimental data and it indicates that the neural network estimated values are close to the experimental data for all data points. Also, the accuracy of the developed network has been tested by using the test data set, which was not used for the training step. In addition, the evaluations indicate that the MSE and MRE for the training data are 0.1954 and 0.0996, respectively, and for the test data are 0.5537 and 0.1460, respectively.

\textbf{Figure 4.} Scatter diagram showing the performance of Eq. (1) for predicting the (liquid-liquid) equilibrium data of the \{\text{nonane (1) + NFM (2)}\} mixture

In the same way, Figures 5 and 6 show a comparison between predicted and experimental data for the LLE characteristics, for \{2,2,4-trimethylpentane (1) + NFM (2)\} and \{heptane (1) + NFM (2)\} mixtures, respectively. The results for the \{2,2,4-trimethylpentane (1) + NFM (2)\} mixture indicate that the MSE and MRE for the training data are 0.0501 and 0.0504, respectively, and for the test data are 1.7624 and 0.3494, respectively. Moreover, it indicates that the MSE and MRE for the training data are 0.9500 and 0.2221, respectively, and for the test data are 7.5888 and 0.7374,
respectively, for the \{\text{heptane (1) + NFM (2)}\} mixtures. This means that the hybrid neural network and the genetic algorithm was also suitable for predicting the data points which are not used in the training data set.

Figure 5. Scatter diagram showing the performance of Eq. (2) for predicting (liquid-liquid) equilibrium data of the \{2,2,4-\text{trimethylpentane (1) + NFM (2)}\} mixture

Figure 6. Scatter diagram showing the performance of Eq. (3) for predicting (liquid-liquid) equilibrium data of the \{\text{heptane (1) + NFM (2)}\} mixture
Conclusion

In the present study, three ANN–GA models were developed for three systems including $N$-formylmorpholine (NFM) with alkanes (heptane, nonane, and 2,2,4-trimethylpentane) in order to predict the temperature ($T$) in liquid-liquid equilibrium conditions. The value of $T$ was used as a function of the primarily influencing parameter, mole fraction of the alkane in light phase ($X_{11}$) and mole fraction of alkane in heavy phase ($X_{12}$) which were considered in the inputs of the networks. In this work, the hybrid neural network and genetic algorithm were successfully applied to estimate the LLE characteristics. Three sets of experimental data points were used for training the feedforward neural network. The best architecture for the network has one hidden layer with two neurons which is obtained by trial and error. GA which can be regarded as one of the most effective techniques is used for optimizing the initial weights and biases of the ANN network. This method was applied as a very useful technique in the design of the network. The performance of the proposed ANN-GA model was also examined through its application in a test data set consisting of about one-third of the experimental data not used for training. The results of applying the hybrid of artificial neural network and genetic algorithm (ANN-GA) model show that the method has a very good performance in estimating the LLE data of the binary systems containing $N$-formylmorpholine.

List of symbols

$\text{b : bias}$
$w : \text{weight}$
$F : \text{transfer function}$
$m : \text{number of input variables}$
$n : \text{number of neurons}$
$N : \text{number of data points}$
$t : \text{target}$
$T : \text{temperature [K]}$
$U : \text{input value of the network}$
$Y : \text{final answer of the network}$

Subscripts

$i : \text{input layer}$
$j : \text{hidden layer}$
$k : \text{output layer}$
References


[34] Haykin S. *Neural Networks*; M. Horton ed., 1999


**How to cite this manuscript:** Reza Beigzadeh. Estimation of LLE Data for Binary Systems of $N$-Formylmorpholine with Alkanes Using Artificial Neural Network–Genetic Algorithm (ANN–GA) Model. Chemical Methodologies 3(1), 2019, 67-82. [DOI: 10.22034/CHEMM.2018.133293.1059]